High Valuations and Low Growth

Low-Frequency Evidence in the Time Series and Cross Section

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Background

Almost 100% of asset pricing:

- Consumption, dividends, prices, wealth are non-stationary...
- ... but cash-flow growth $\Delta c_t, \Delta d_t$ and returns $r_t$ are stationary
- ... and prices and cash flows are cointegrated, so valuation ratios $(p_t - d_t, w_t - c_t)$ are stationary
- Then all questions are effectively about deviations from long-run means
  - E.g., risk premia $\iff$ second moments, $\mathbb{E}[r_i - r_f] \leq -\text{Cov}(M, r_i - r_f)$
- Similar to (often overlapping with) the focus of business-cycle research
- Source of real controversy and debate in 1980s
- Since then, not much discussion (a little around tech bubble, not a ton since)
Background

Today:

- Does it make sense to revisit these issues?
- First-order questions (literally)
- Logically impossible to get dispositive evidence in either direction
- But still some interesting features of the data
- Will first present a bunch of basic empirical facts (some collected myself, some from other papers)
- Then: implications and questions arising within basic structural frameworks
1. Empirical Facts
   Valuations
   Yields
   Output & Cash Flows

2. Decompositions & Implications

3. Conclusion
Long-Run Empirical Facts: Valuations

Price-Dividend Ratio

Annual, U.S. (CRSP)

Note: End-of-year market cap divided by total dividends for prior 12 months.
Long-Run Empirical Facts: Valuations

Price-Dividend Ratios

Source: Golez and Koudijs (2018), CRSP.
Long-Run Empirical Facts: Valuations

Price to 10-Year Earnings

Source: Robert Shiller. Figure shows real S&P 500 price to 10-year real earnings (CAPE).
Long-Run Empirical Facts: Valuations

Wealth-consumption ratio from Duffee (2005) [series end 2001]:

A. Stock market wealth/consumption

B. Detrended consumption-wealth ratio

Figure 2. Ratios of wealth to consumption. The top panel plots the ratio of the market capitalization of publicly traded stocks to total consumption on nondurables and services. The bottom panel plots the detrended consumption–wealth ratio introduced in Lettau and Ludvigson (2001).
Long-Run Empirical Facts: Yields

International evidence from Kuvshinov and Zimmermann (2020a) [note ratio inverted relative to previous slides & includes real-estate valuations]:

Figure 1: The risky asset yield

Notes: Data for 17 countries. The yield is the average of the dividend-price and rent-price ratios. The solid line and the shaded area are, respectively, the mean and interquartile range of the individual country data in each year. The dashed line represents the linear trend.
Long-Run Empirical Facts: Yields

Real rates from Schmelzing (2020):

Trend decline:

- All-time (1317-): \(-1.59\text{bps p.a.}\)
- Post Bullion famine (1494-): \(-1.36\text{bps p.a.}\)
- North-Weingast (1694-): \(-1.44\text{bps p.a.}\)
- Post-Napoleonic (1820-): \(-2.29\text{bps p.a.}\)

Figure IV: Headline global real rate, GDP-weighted, and trend declines, 1317-2018.
Long-Run Empirical Facts: Yields

Nominal rates from Miller, Paron, and Wachter (2020) via Schmelzing:

Figure 1: Nominal government rates
Long-Run Empirical Facts: Output & Cash Flows

U.S. Real GDP Growth

Notes: Moving average uses Gaussian kernel weights with 15-year bandwidth. Both series calculated using BEA yearly log real GDP growth.
Long-Run Empirical Facts: Output & Cash Flows

Log Real Output and Trough-to-Peak Trend

- Graph showing the Log Real Output and Trough-to-Peak Trend from 1960q1 to 2020q1.
Long-Run Empirical Facts: Output & Cash Flows

U.S. Real GDP and Dividend Growth

- - - 5-Year Annual Growth

Moving Average

Memo: Moving Average CRSP Dividend Growth

Notes: Moving average uses Gaussian kernel weights with 15-year bandwidth. Both series calculated using BEA yearly log real GDP growth.
Holds using aggregated IBES forecasts of long-term growth as well.
Long-Run Empirical Facts: Output & Cash Flows

- World Output Growth

15Y Kernel MA Real GDP Growth

- 1850
- 1900
- 1950
- 2000
Initial Takeaways

1. Valuations and cash-flow growth are moving in “wrong” direction relative to one another
   - And series fail standard stationarity tests at 5% level, for what it’s worth
   - Some of the effect is compositional: listed firms are different now (more repurchases, higher profit share) than in the past
   - Will show more on this in a bit

2. Interest rates seem to be declining fairly steadily
   - Can’t literally be trending down (or have neg. drift) over very long run

Next: What it means and how to make sense of it

   - Time-series decompositions: Long-run vs. transitory components of valuation and cash flows
   - Cross-sectional decompositions: Valuation changes within firm vs. reallocation across firms
   - Implications

Complementary recent work: Greenwald, Lettau, Ludvigson (2021); van Binsbergen (2020); Farhi and Gourio (2018)
Outline

1. Empirical Facts

2. Decompositions & Implications
   Time Series
   Cross Section

3. Conclusion
Time-Series Decomposition

Two cases:

1. Standard: Stationary growth and valuation
   - Log dividend growth $g_t = \Delta d_t$ and equity return $r_t$ are stationary
   - Campbell-Shiller decomposition:

$\begin{align*}
d_t - p_t & \equiv dp_t = k + \mathbb{E}_t \sum_{j=0}^{\infty} \rho^j [r_{t+1+j} - g_{t+1+j}] \\
& = \overline{dp} + \mathbb{E}_t \sum_{j=0}^{\infty} \rho^j [(r_{t+1+j} - \bar{r}) - (g_{t+1+j} - \bar{g})],
\end{align*}$

where $\overline{dp} = \log \left( \frac{\exp \bar{r} - \exp \bar{g}}{\exp \bar{g}} \right) \Rightarrow \exp(\overline{dp}) \approx \bar{r} - \bar{g}$
Time-Series Decomposition

Two cases:

2. **Alternative**: Non-stationary growth and valuation

   - Log dividend growth $g_t$, equity returns $r_t$ have martingale components:
     
     $$g_t = \bar{g}_t + \eta_{g,t}, \quad r_t = \bar{r}_t + \eta_{r,t},$$
     
     $$E_t[\bar{g}_{t+1} - \bar{g}_t] = E_t[\bar{r}_{t+1} - \bar{r}_t] = 0 = E_t[\eta_{g,t+1}] = E_t[\eta_{r,t+1}]$$

   - Modified decomposition based on Lettau and Van Nieuwerburgh (2008):
     
     $$dp_t = \overline{dp}_t + E_t \sum_{j=0}^{\infty} \rho^j [(r_{t+1+j} - \bar{r}_t) - (g_{t+1+j} - \bar{g}_t)],$$
     
     where $\overline{dp}_t = \log \left( \frac{\exp \bar{r}_t - \exp \bar{g}_t}{\exp \bar{g}_t} \right) \implies \exp(\overline{dp}_t) \approx \bar{r}_t - \bar{g}_t$

   - In fact a generalization of stationary case
Time-Series Decomposition

\[ \exp(dp_t) \approx \bar{r}_t - \bar{g}_t \]  

(1)

\[ dp_t - \bar{dp}_t = \mathbb{E}_t \sum_{j=0}^{\infty} \rho^j [(r_{t+1+j} - \bar{r}_t) - (g_{t+1+j} - \bar{g}_t)] \]  

(2)

1. **Shifting steady states** $\bar{dp}_t, \bar{r}_t, \bar{g}_t$: Measure using kernel-weighted average
   - Gaussian kernel (\(\sim\) exponentially weighted moving average)
   - 15-year bandwidth (centered \(\pm\)7.5 years, truncated at each end, and then shifted to end of window)
   - Forecasting regressions for $\bar{r}_{t+15}, \bar{g}_{t+15}$ on $\bar{dp}_t$

2. Forecasting regressions for stationary components (relative to $\bar{r}_t, \bar{g}_t$)
Time-Series Decomposition: Results

\[ \exp(dp_t) \approx \bar{r}_t - \bar{g}_t \]  
(1)

\[ dp_t - \bar{dp}_t = \mathbb{E}_t \sum_{j=0}^{\infty} \rho^j [(r_{t+1+j} - \bar{r}_t) - (g_{t+1+j} - \bar{g}_t)] \]  
(2)

Forecasting Regressions: Returns and CRSP Dividend Growth

<table>
<thead>
<tr>
<th>Regressions for:</th>
<th>( \bar{r}_{t+15} )</th>
<th>( \bar{g}_{t+15} )</th>
<th>( \sum_{j=0}^{15} [(r_{t+1+j} - \bar{r}_t)] )</th>
<th>( \sum_{j=0}^{15} [(g_{t+1+j} - \bar{g}_t)] )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \exp(dp_t) )</td>
<td>0.70 (2.3)</td>
<td>0.85 (3.1)</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>1.38 (5.7)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>-0.35 (-1.5)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>( R^2 )</td>
<td>0.16</td>
<td>0.25</td>
<td>0.03</td>
<td>0.19</td>
</tr>
</tbody>
</table>

Notes: Heteroskedasticity- and autocorrelation-robust t-statistics in parentheses, estimated via equal-weighted periodogram estimator using 6 periodogram ordinates [Lazarus, Lewis, Stock (2021)]. \( N = 95 \).

Holds as well using total payouts (incl. net repurchases), output growth, consumption growth
Time-Series Decomposition: Results

\[ \exp(d p_t) \approx \bar{r}_t - \bar{g}_t \]  

\[ d p_t - \bar{d} p_t = E_t \sum_{j=0}^{\infty} \rho^j [(r_{t+1+j} - \bar{r}_t) - (g_{t+1+j} - \bar{g}_t)] \]  

Variance Decomposition for \( dp_t \) Components

<table>
<thead>
<tr>
<th>Percent explained by:</th>
<th>Returns</th>
<th>Dividend Growth</th>
</tr>
</thead>
<tbody>
<tr>
<td>Martingale</td>
<td>70</td>
<td>85</td>
</tr>
<tr>
<td>Deviation</td>
<td>138</td>
<td>-35</td>
</tr>
</tbody>
</table>
Time-Series Decomposition: Results

Future Output Growth and Dividend Yield

Stochastic Trends

15-Year-Ahead Trend Growth
D/P
Time-Series Decomposition: Implications

Helps explain failure of return forecasting regressions out of sample using \( dp_t \) [as pointed out by Lettau and Van Nieuwerburgh (2008)]:

- If \( dp_t \) keeps hitting historic lows, an out-of-sample forecasting model will keep telling you to expect negative equity returns if you’re assuming stationarity.

- Table from Goyal and Welch (2008):

<table>
<thead>
<tr>
<th>Variable</th>
<th>Log returns (IS)</th>
<th>OOS (IS)</th>
<th>Simple returns (Campbell and Thompson (2005) OOS)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>( \hat{\alpha}^2 )</td>
<td>( \hat{\beta}^2 )</td>
<td>( \hat{\gamma}^2 )</td>
</tr>
<tr>
<td>( \Delta c )</td>
<td>0.02</td>
<td>-0.10</td>
<td>-0.10</td>
</tr>
<tr>
<td>( \text{svar} )</td>
<td>-0.09</td>
<td>-0.07</td>
<td>-0.07</td>
</tr>
<tr>
<td>( \text{dif} )</td>
<td>-0.02</td>
<td>-0.07</td>
<td>-0.08</td>
</tr>
<tr>
<td>( \text{ltv} )</td>
<td>-0.03</td>
<td>0.02</td>
<td>0.02</td>
</tr>
<tr>
<td>( \text{ltr} )</td>
<td>0.04</td>
<td>0.07</td>
<td>0.08</td>
</tr>
<tr>
<td>( \text{inf} )</td>
<td>-0.01</td>
<td>0.14</td>
<td>-0.05</td>
</tr>
<tr>
<td>( \text{tms} )</td>
<td>0.12</td>
<td>0.18</td>
<td>0.20</td>
</tr>
<tr>
<td>( \text{tbf} )</td>
<td>0.10</td>
<td>0.20*</td>
<td>0.15</td>
</tr>
<tr>
<td>( \text{dyf} )</td>
<td>-0.06</td>
<td>0.28*</td>
<td>0.28</td>
</tr>
<tr>
<td>( \text{dp} )</td>
<td>0.12</td>
<td>0.35*</td>
<td>0.29</td>
</tr>
<tr>
<td>( \text{dy} )</td>
<td>0.25*</td>
<td>0.49***</td>
<td>0.45</td>
</tr>
<tr>
<td>( \text{ep} )</td>
<td>0.51**</td>
<td>0.52**</td>
<td>0.45</td>
</tr>
<tr>
<td>( \text{eis} )</td>
<td>0.82***</td>
<td>0.80***</td>
<td>0.59</td>
</tr>
<tr>
<td>( \beta )</td>
<td>0.45**</td>
<td>0.81***</td>
<td>0.88</td>
</tr>
<tr>
<td>( \text{efp} )</td>
<td>0.46**</td>
<td>0.86***</td>
<td>0.96</td>
</tr>
<tr>
<td>( \text{csp} )</td>
<td>0.92***</td>
<td>0.95***</td>
<td>0.93</td>
</tr>
<tr>
<td>( \text{ntis} )</td>
<td>0.94**</td>
<td>1.02**</td>
<td>0.88</td>
</tr>
<tr>
<td>( \text{cay3} )</td>
<td>1.88***</td>
<td>1.87***</td>
<td>1.57</td>
</tr>
</tbody>
</table>

\( \text{T} \) refers to the in-sample forecast model and \( \text{OOS} \) refers to the out-of-sample forecast model. The table reports the forecast error variance ratio (FEVR) and the coefficient of determination (R²) for each variable. Positive values indicate that the forecasting model overstates the forecast error variance, while negative values indicate that the forecasting model understates the forecast error variance. ** indicates significance at the 5% level, *** indicates significance at the 1% level.
Implications

As a thought exercise:

▶ Assume conditional log-normality & homoskedasticity, Epstein-Zin preferences, but declining consumption growth:

\[ c_t - w_t = \text{const}_t + \mathbb{E}_t \sum_{j=0}^{\infty} \rho_{t+j} (r_{t+1+j} - \Delta c_{t+1+j}) \]

\[ = \text{const}_t + \left(1 - \frac{1}{\psi}\right) \mathbb{E}_t \sum_{j=0}^{\infty} \rho_{t+j} \Delta c_{t+1+j} \]

long-run growth

▶ Declining long-run growth increases valuations (decreases \( c_t - w_t \)) iff \( \psi = \text{IES} < 1 \)

▶ Then discount rates more than offset declining growth (and equity market duration significantly lengthens, as it has in the data)
Cross-Sectional Decomposition

Is the story plausible?

- In aggregate, can have discount rate effect overwhelm (negative) growth effect in GE

- But what about for a single firm?

- Consider book to market, since some firms pay no dividends (aggregate decline in log book-to-market of about 2.5% per year since 1980)

- Decompose aggregate book-to-market changes into within-vs.-across firm. Roughly, for aggregate book to market $\theta_t$, firm shares $\{\sigma_{j,t}\}$:

\[
\Delta \theta_{t+1} = \sum_{j=1}^{n} (\theta_{j,t+1} - \theta_{j,t}) \sigma_{j,t+1} + \sum_{j=1}^{n} (\sigma_{j,t+1} - \sigma_{j,t}) \theta_{j,t}
\]

- Using CRSP/Compustat data: Within (first term): +0.2%/yr since 1981. Across: −3.6%! (Small remainder is entry/exit)

- So the entire increase in valuations (decline in B/M) can be explained in the cross-section with a compositional change from low- to high-valuation firms, but the average firm has a stable B/M! Market was GM, now is Tesla
Cross-Sectional Decomposition


- **Within a Firm**
- **Across Firms**
- **Total**

Log Cumulative Change

Cross-Sectional Decomposition: More Evidence
Cross-Sectional Decomposition: More Evidence

Percent of CRSP Firms with Negative Annual Accounting Earnings
Next: Model

Want to consider a disaggregated model where:

1. The composition of public equity is changing over time
   - The average firm is now a long-duration firm: high intangibles, high markups

2. Offsetting effects: shift to these higher-productivity firms increases growth all else equal...

3. but the shift is spurred by a decline in firm-level productivity growth, whose effect is bigger than the reallocation effect
   - Alternative view: increasing appropriability of growth options by long-duration firms (which then further drags down $g$), …
Outline

1. Empirical Facts

2. Decompositions & Implications

3. Conclusion
Additional Implications and Final Thoughts

- Slight *decline* in within-firm valuation ratio implies (a) lower within-firm growth prospects or (b) higher expected returns
  - Either way, suggests aggregate equity valuations have increased *less* than expected given decline in interest rates
  - In line with evidence presented in van Binsbergen (2020): Equity has underperformed relative to duration-matched fixed income

- Additional evidence: Greenwald, Lettau, Ludvigson (2021) estimate that a big portion of the increase in valuations is from reallocation of output from workers to capital owners
  - Further lines up nicely with evidence here if there’s been a reallocation from high- to low-labor-share firms...which there has, as Vincent and Kehrig (2021) show (and within-establishment change is again actually positive)

- A ton to be done
  - Questions are really fundamental: Smith, Marx, Ricardo argued over long-run growth declines & implications